Sputnik: a Stochastic Petri Net Library in Python

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1. Installation

Sputnik encompasses a range of tools that allow the design, simulation and analysis of stochastic Petri nets. Sputnik is written for use with Python version 2.7 and has been tested on both Linux and OSX operating systems. It has the following dependencies:

Essential libraries: NumPy, *†* Scipy, *†* matplotlib, *†* gtk, pygtk. Optional libraries: libsbml - Required if SBML import functionality is desired

[†]We recommend using the Enthought Python Distribution which is free for academic use and includes Python 2.7.2, NumPy, Scipy and matplotlib.

Having downloaded the latest version of Sputnik from [https://github.com/sputnikpetrin](https://github.com/sputnikpetrinets/project_sputnik/)ets/ [project_sputnik/](https://github.com/sputnikpetrinets/project_sputnik/), first extract the files using the following command:

> unzip project_sputnik-master.zip

To run the GUI, simply call python run-sputnik.py from the project sputnik-master directory. To import the library for use in other Python scripts, move the directory to somewhere on your PYTHONPATH. Similarly, to make the GUI accessible system-wide, move the directory to one listed in your shell's PATH.

2. Quick start

To jump into the program without reading the full documentation, follow this short vignette which is explained in more detail in section [6.1.](#page-30-1)

- 1. Open the Sputnik GUI with python start.py
- 2. Use \mathbf{U} to open the repressilator.txt file found in the examples/ directory.
- 3. View the calculated net invariants with \int .
- 4. Open the simulation \ll options, set Runtime to, for example, 100000 and Time-Step to 500 and click Start Simulation.
- 5. After a few seconds, an info-box will inform you the simulation is finished, click Close.
- 6. Now in the lower-right Places pane, uncheck 'Plot' for all places except pA, pB and pC — these are the three proteins of interest. Click Show Plot to see the results.
- 7. Optionally, use the various plot settings to add a title, choose custom line colours and edit legend-text and use the plot window dialogue to save the simulation plot.
- 8. Repeat the simulation by increasing the Number of Simulations to 4. Check the Create subplots checkbox and enter 2 in Subplot Rows and Columns to create a 2×2 plot of all four simulations — highlighting the stochastic variation between runs.
- 9. Close the Simulation window and click to view a token game animation of simulated Petri net events. Click OK to use the default parameters.
- 10. The play \bullet button will then step through the simulation, highlighting firing transitions in red and updating the place markings as tokens are exchanged. You can also pause $\overline{\mathbf{0}}$ and step through each event using $\overline{\mathbf{0}}$ and $\overline{\mathbf{0}}$.

For more detailed examples and a full explanation of Sputnik's features and capabilities, consult sections [4,](#page-7-0) [5](#page-13-0) and [6.](#page-30-0)

3. Introduction

Petri nets^{[\[1\]](#page-43-0)} are a versatile and understandable graph notation which can be used to represent many kinds of network. They offer an unambiguous mathematical framework to describe a system, as well as providing the means to test hypotheses regarding its behaviour and properties^{[\[2\]](#page-43-1)}. Having evolved in mathematics and computer science^{[\[3\]](#page-43-2)}, Petri nets have more recently been used by systems biologists for the purpose of modelling biological systems $[4,5,6]$ $[4,5,6]$ $[4,5,6]$. Stochastic Petri nets are a form of Petri net suitable for simulating systems with stochastic mass action kinetics. They are therefore a convenient way to represent and simulate systems where low species abundances result in appreciable intrinsic noise^{[\[7\]](#page-43-6)}. Such systems include gene regulatory networks, signalling systems, and many metabolic networks.

A Petri net consists of four types of element: places, transitions, arcs and tokens. Places are nodes representing the components of a system, while transitions represent reactions or events. Arcs are directed edges that connect the two. Each arc is associated with an integer weight representing the stoichiometry of the transitions. The state of the system is given by the distribution of tokens among the places; the number of tokens possessed by a place is known as its marking. The firing of a particular transition, known as an "event", moves tokens between places as directed by the pre and post arcs, changing the "global marking" of the system. A particular transition is "enabled" only if the markings of all its input places at least equal the weights of the corresponding pre arcs. Places may have a "capacity", a maximum number of tokens that can be possessed by the place. "Test arcs" and "inhibitory arcs", which represent minimum and maximum marking conditions respectively, may provide additional checks on whether a particular transition is enabled, but do not directly result in the consumption of tokens. The "*P*-invariants" of a net are combinations of places with a constant total marking, while the "*T*-invariants" are patterns of transition firings that leave the global marking unchanged^{[\[8\]](#page-43-7)}. Firings are probabilistic and associated with stochastic rate constants, with exponentially distributed waiting times between events^{[\[2\]](#page-43-1)}.

Here we present a Python library, Sputnik that provides a range of tools for constructing, visualising, analysing and simulating stochastic Petri nets, accessible either from the command-line or from a user-friendly GUI. Petri net models may be imported from file, or created *de novo* using the Petri net editor. Automatic layouting of the nets is achieved via a choice of drawing algorithms, while net components can also be manually repositioned for fine-tuning. Petri nets may be simulated by either of two stochastic simulation algorithms, the Gillespie^{[\[9\]](#page-43-8)} or the tau-leap^{[\[10\]](#page-43-9)}, and the resulting timecourses can be visualised in customisable plots. Net properties such as the *P*- and *T*-invariants, the stoichiometry matrix and the dependency matrix can also be calculated.

In addition to defining a TXT format for storing Petri net models, Sputnik also supports the systems biology exchange formats Systems Biology Markup Language (SBML)^{[\[11\]](#page-44-0)} and Petri Net Markup Language $(PNML)^{[12]}$ $(PNML)^{[12]}$ $(PNML)^{[12]}$. Petri nets may be saved or retrieved in any of these three file formats, ensuring cross-compatibility with the growing body of systems biology software already available. Petri net visualisations may be exported in a variety of common image formats, and the layout coordinates may additionally be saved to file, to be re-imported the next time the Petri net is loaded. Simulation visualisations may also be saved, or the raw data exported for further analysis. A basic data flow diagram describing these processes is shown in Figure [3.1.](#page-6-0)

Figure 3.1: A basic data flow diagram showing the library's inputs, outputs and core internal structure. The two core data containers, PetriNet and PetriNetData, are further discussed in sections [5.3](#page-17-0) and [5.4](#page-18-0)

We advise that you read through the Examples to get a feel for how the library works: For full instructions on using the GUI, see Chapter [4;](#page-7-0) if you prefer to write your own scripts, see Chapter [5](#page-13-0) for documentation covering the relevant methods and variables.

4. Using the library: GUI

All Sputnik functionality is readily accessible through the graphical user interface (GUI). Figure [4.1](#page-7-1) shows a general view of the main window of the GUI.

Figure 4.1: The main window of the GUI, shown displaying the "Repressilator" $model^[13]$ $model^[13]$ $model^[13]$.

All of the library's capabilities can be accessed quickly and easily, via the row of icons in the menu bar above the drawing area. All of the icons used are freely available for private and commercial use under a Creative Commons Attribution-Share Alike^{[\[14\]](#page-44-3)} (CC BY-SA 3.0) license from the Open Icon Library^{[\[15\]](#page-44-4)}. Table [4.1](#page-8-0) provides a short explanation for each of the icon buttons in the main window (Figure [4.1\)](#page-7-1).

Icon	Shortcut	Description
	$Ctrl + O$	Open Petri net
$\begin{array}{c} x & x \\ x & x \\ x & x \end{array}$	$Ctrl + I$	Open layout
m	$Ctrl + S$	Save Petri net
	$Ctrl + E$	Save layout
$\frac{1}{8}$	$Ctrl + P$	Export Petri Net
	$Ctrl + Z$	Undo
O O X	Del	Delete
	$-$ (minus)	Zoom out
	$+$ (plus)	Zoom in
	$Ctrl + C$	Copy
\bigcup	$Ctrl + V$	Paste
	F5	Refresh
R SOP R	$Alt + L$	Layout algorithms
	$Alt + D$	Simulation plot
	$Alt + I$	Calculate invariants
2 4 5	$Alt + G$	Token Game simulation
$\circledcirc \circledcirc \circledcirc$	В	Previous step
	$_{\rm R}$	Play
	\mathbf{P}	Pause
	S	Stop
	F	Next step
	$Ctrl + L$	Lock
	$_{\rm F6}$	Add Place
	F7	Add Transition
$\ddot{}$	F8	Add Standard Arc
\sim	F9	Add Inhibitory Arc
	F10	Add Test Arc
\bigcirc	$Alt + F4$	Exit
	Esc	Abort

Table 4.1: Summary of the button icons found in the GUI main toolbar

4.1 Basic functions

Loading and saving Petri nets can be loaded **from** *TXT*, *PNML* or *SBML* files, and saved \Box in any of these formats. The current layout can be saved to file \Box and loaded again in the future. The visualisation of the net can be saved as an image file, in PDF, PS or SVG format.

Visualisation On loading a file, the Petri net will be laid out by a spectral graph drawing algorithm using the default settings. To configure the layout, click $\frac{\infty}{2}$ to open the layout window. *W idth* and *Height* determine the drawing area size, while the *Border* option prevents net components from being drawn too close to the edges of the drawing area. *Displacement Radius* defines the minimum distance between components. Components can also be positioned manually by clicking and dragging. Multiple components can be selected at once by holding Ctrl while drawing a box around an area. Zoom in and out using \mathcal{L} and $\mathcal P$.

Editing the Petri net Add components by clicking on the correct icon (place \circlearrowright : transition \Box ; standard arc $\ddot{}$, test arc $\ddot{}$; inhibitory arc $\ddot{}$ and then clicking to place the component on screen. When placing arcs, the first click places the start of the arc and the second click places the arrow head end. Standard arcs must connect a place to a transition or vice versa, while other arcs must connect a place to a transition only; acceptable connections will be highlighted green, unacceptable connections red. Components can be copied and pasted either using keyboard shortcuts or by clicking on \Box and \Box . The copied component will be overlaid on the original, ready to be manually repositioned. Components can be deleted using Del or clicking \mathscr{R} . Deleting a place or transition will also delete the arcs connected to it. Click \Box to lock the current state, and to \Box undo an action. To modify a component, double click the component to bring up a properties window and enter the desired changes.

P- and *T*-invariants Calculate and display the invariants by clicking $\vert \cdot \vert$.

Animation To display an animation of the Petri net simulated by the Gillespie algorithm, click . The animation shows each iteration of the simulation, highlighting the event that occurred. The transition, place(s) and arc(s) involved are highlighted in red, and the markings are updated appropriately. The animation is controlled by a player-like menu, giving options to jump forward (Θ) or backward (Θ) one iteration, play continously (Θ), pause ($\mathbf{0}$), or stop ($\mathbf{0}$). There is also a progress bar displayed below the icons, which can be clicked to jump to a specific position in the simulation. Figure [4.2](#page-10-0) shows a view of an animation of the Lotka-Volterra model in progress.

Figure 4.2: Petri net simulation animation The "predation" transition, which involves both places, "X1" and "X2" is firing.

4.2 Simulation

Figure [4.3](#page-11-1) shows the simulation window.

Figure 4.3: Simulation window showing simulation and plotting options.

Simulation options In most cases the Gillespie algorithm should be used, and the only settings to adjust are *Run Time* and *Time Step*. Multiple runs can be carried out at once by changing the *Number of Simulations* option. See section [5.7](#page-24-1) for information on selecting a simulation algorithm and adjusting simulation parameters.

Plot options These options control settings for the whole plot, such as title, line width and axis labels. Legend position is controlled in the same way as for the matplotlib package. Save alterations by clicking *Save Settings*. The default is a single plot; create subplots by checking the *Create Subplots* button.

Subplot options These options control the settings for each individual subplot. If multiple simulations have been performed when the "Create Subplots" option is selected, each simulation will be rendered as a subplot. If only one simulation was run, subplots will be generated for each species' timecourse. Save alterations by clicking *Save Settings*.

Line options These options settings for each invididual timecourse within a plot, for example line colour and the label to be displayed in the legend. Checkboxes determine which timecourses to plot. To customise line colour, deselect the *Automatic Colour Allocation* checkbox and then use the colour selector. Save alterations by clicking *Save Settings*.

5. Using the library: command-line

5.1 Help documentation

 $PyDoc^[16]$ $PyDoc^[16]$ $PyDoc^[16]$ is a module within Python used for documentation purposes. It generates documentation for classes and modules automatically from "docstring" comments within the code and can be displayed on the console, exported as HTML files or handed directly to a Web browser.

The *documentation* folder contains PyDoc-generated HTML files providing extensive documentation for all the classes, methods and variables of the Sputnik code. To consult PyDoc documentation from within the Python Interactive Environment, issue one of the commands:

```
\ begin { small } 1
# For information about a specific class:
help(<module name>.<ClassName>) 3
                                        4
\# For information about a specific method:
help(<module name>.<ClassName>.<method name>) 6
                                        7
\langleend\{small\}
```
5.2 Import and export of Petri nets

5.2.1 Loading a Petri net

In Sputnik, file input is parsed to PetriNetData via:

8 9 >>>>< RLexerTxt >>>>= ! RParser *P etri net T okens Input f ile* ! ! *P etri Net Data* RLexerSBML >>>>; RLexerPNML >>>>:

Loading a Petri net in this way, through iPython or using a script, requires the import of two classes, a general parser RParser() and a lexer that is specific to the file type you are opening, i.e. RLexerTxt(), RLexerSBML() or RLexerPNML(). As an example, the following commands will parse a .txt file to a PetriNetData object p:

```
import sputnik io 11 metatra. Na matamatan na kasa na matamatan na kasa na matamatan na kasa na matamatan na m
                                                            \overline{2}lexer = sputnik io . RLexerTxt () 3
parser = sputnik io . RParser () 4
input file = open('examplefile.txt')tokens = lexer.lex ( inputfile ) 6
parser. data = tokens
parser . parse () 8
p = parser. output
```
5.2.2 Saving a Petri net

In order to save a Petri net stored in a PetriNetData object p, the following process is implemented:

To perform these actions as part of a script, for example to save to PNML format, the following commands can be issued:

```
import sputnik<sub>-10</sub>
                                                                               2
\text{converter} = \text{sputnik\_io} \cdot \text{WConverterPNML}(p) 3
converter . save ('output filename . pnml')
```
5.2.3 Text format specification

Writing a plain text file is often the fastest way to define a new Petri net for use with **Sputnik**. The text format closely mirrors a mathematical Petri net definition, and is specified below.

Places – a list of strings that represent identifiers for each Petri net place.

Required: Yes Syntax: p / places Example: $p = [prey, predator]$

Transitions – a list of strings identifying transition names.

Required: Yes Syntax: t / transitions Example: $t = [preyBirth, predation, predatorDeath]$

Pre – a matrix describing the weights of arcs connecting places to transitions. Required: Yes Syntax: pre / pre arcs / pre arcs Example: pre = [[1,0],[1,1],[0,1]]

Post – a matrix describing the weights of arcs connecting transitions to places. Required: Yes Syntax: post / post arcs / post arcs Example: $post = [[2,0],[0,2],[0,0]]$

Initial marking $-$ a list of integers that count the number of tokens in each place prior to simulation. Should be the same length as places.

Required: No (set to 0 if absent) Syntax: m / markings Example: m = [100,20]]

Rates – a list of numbers that represent the stochastic rate constants associated with each transition. Required: No (set to 0 if absent) Syntax: r / rates Example: $r = [1, 0.005, 0.6]$

- **Capacities** a list of integers defining the maximum number of tokens allowed in each place. If present, must have the same length as places. Required: No Syntax: c / capacities Example: c = [500,500]
- Inhibitory arcs a matrix describing a logical test performed on place markings to enable or disable a transition. Transitions will not fire if stated markings are above the values stated in this matrix (zeros are ignored), otherwise they fire as normal. Required: No Syntax: i / inhib / inhibitory arcs / inhibitory arcs Example: inhib = [[600,0],[0,0],[400,0]]
- Test arcs a matrix describing a logical test performed on place markings to enable or disable a transition. Transitions will not fire if stated markings are below or equal to the values stated in this matrix, otherwise they fire as normal.

Required: Yes

Syntax: test / test arcs / test arcs

Example: test = [[2,0],[2,0],[0,2]]

5.2.4 Standalone file conversion

Standalone file conversion can be performed using fconvert. This must be run with two parameters, input and output filenames (relative or absolute paths), in the form:

\$./fconvert inputfile.txt outputfile.xml

File extensions .txt, .sbml, .pnml and .xml are automatically detected, otherwise the user will be prompted to state the file type.

Note: the ability to read and write SBML requires the freely avalaible libSBML Python API (http://sbml.org/Software/libSBML/docs/python-api/).

5.3 Manually inputting a Petri net

A stochastic Petri net is defined by the *n*-tuple $N = \{P, T, Pre, Post, M_0, R, C^*, Test^*,\}$ *Inhib*^{*}*}*, where the starred elements are optional. A Petri net model may be input manually, by creating a sputnik petrinet. PetriNetData() object and then setting its instance variables as the appropriate NumPy matrices and arrays. The *Pre* and *Post* matrices are stored in a sputnik petrinet.Stoich() object that is set as the stoichiometry instance variable of the PetriNetData() object. Refer to the TXT input format specification for the required dimensions of the data elements. A PetriNetData object p should be created using the following template:

```
import numpy as np
import sputnik petrinet 2000 and 
                                                                                     3
p =sputnik_petrinet. PetriNetData()
p. stoichiometry = sputnik_{petrinet}. Stoich()
p. stoichiometry . pre_arcs = np . matrix(<post_arc_matrix>, dtype=int 6
    )
p. stoichiometry . post arcs = np . matrix(\langle post arc matrix\rangle, dtype= 7
    int )
                                                                                     8
p. places = np.array(<i>place_labels</i>)p. transitions = np. array(< transition labels >) 10p \text{. rates} = np \text{. array}(\text{<rates} >, dy) p \text{.} false (11
p. initial_marking = np. array(\langle initial_marking >, dtype=int) 12
                                                                                     13
```


5.4 Create a PetriNet object

Whereas the PetriNetData object created in the above sections contains a mathematical representation of a Petri net (data elements are matrices and arrays), a PetriNet object contains representations of each individual component (place, transition or arc) which each have certain properties (labels, markings, rates, weights etc.). PetriNet objects are used by the visualisation part of the library, while the simulation, invariant calculation and parsers use PetriNetData objects. The corresponding PetriNetData object of a PetriNet object is accessed through its petrinetdata variable. All component classes inherit from a general Component parent class.

To create a PetriNet object pn from a PetriNetData object pn:

```
## i n s t a n t i a t e a P e t r iN e t o b j e c t 1
p_n = s put nik _ petrinet . PetriNet () 2
                                                                    3
# assign the PetriNetData object
pn. petri.net_data = p6
# create the components
pn. convert_components ()
```
5.4.1 Edit a PetriNet object

The framework permits individual components to be instantiated from the command line and added to a PetriNet object. After editing a Petri net in this way, the PetriNet class method convert matrices() method must be run to update the corresponding PetriNetData object. Example code is presented below for completeness, although we strongly suggest the user either uses the GUI for this, or just alters the PetriNetData properties directly, then reruns the converter to update the components. Another simple solution would be to alter a *TXT* input file appropriately and then reimport it.

```
import sputnik_petrinet
                                          2
## create the single components of a petri net
                                          4
## c r e a t e a p l a c e 5
p = sputnik_petrinet.Place ([100.0, 50.0], 15., [0., 0., 0.], 6
  [255., 255., 255.]p. \text{label} = "Place" 7
p \cdot \text{key} = "Place"p. marking = <marking> 9
                                          10
## c r e a t e a t r a n s i t i o n 11
t = sputnik petrinet . Transition ([50.0, 50.0], [15, 30], [0., 0., ][0.], [0.], 0.], 0.]t. label = "Transition" 13
t \cdot key = "Transformation" 14
t. rate = <rate> 15
                                          16
## create a pre arc that connects the place and transition in
a = \text{sputnik\_petrinet}. Arc () 18
a. line_type = sputnik_petrinet. Arc. LINE_TYPE_STRAIGHT 19
a. \text{label} = \text{str}('') 20
a. \text{key} = "StandardArc"a. origin = p 22
a. target = t 23
a. weight = \langleweight\rangle 24
                                          25## Other constructors: TestArc (), InhibitoryArc () 26
## O ther l i n e t y p e s : LINE TYPE ARC UPPER , LINE TYPE ARC LOWER 27
                                          28
# instantiate a PetriNet object 29
p_n = s put nik petrinet . PetriNet () 30
```


5.5 Petri net visualisation

5.5.1 Obtaining Petri net layout coordinates

Spectral algorithm

To obtain raw layout coordinates for a PetriNetData object p:

```
import spectral a 1
                                            2
v = spectral_a \cdot Spectral() 3
v. petri net = p 44v. get_{p}etri_{net}()6
## OPTIONAL 7
v. width = \langle \text{width} \rangle ## \text{Default} = 1000
v. height = \langle \text{height} \rangle ## \text{Default} = 1000 9
v. border = \langleborder\rangle ## Default = 20
v.d_radius = \langled_radius\rangle ## Default = 60 11
                                            <sub>12</sub>
coordinate = v. calculate() 13
```
The width, height, border and d_radius variables have default values within the spectral a class but can be overridden if the user desires.

Force-directed algorithm

For the force directed algorithm the process is the same other than the iterations variable can also be optionally set:

```
import force<sub>-a</sub>
```

```
2
v = force_a. ForceDirected () 3
v. petri_net = p
v.get{\text{-}}petr1{\text{-}}net()\epsilon## OPTIONAL 7
v. width = \langle \text{width} \rangle ## \text{Default} = 1000
v. height = \langle \text{height} \rangle ## \text{Default} = 1000 9
v. border = \langleborder> ## Default = 20 10
v. iterations = \langle iterations \rangle ## \textit{Default} = 50 11
                                                       <sub>12</sub>
coordinates = v. calculate()
```
The number of iterations required to reach an acceptable layout varies between graphs. For small graphs (on the order of tens of vertices) 100 iterations may be sufficient, for graphs containing hundreds of vertices a thousand or more iterations may be required. Some trial and error may be required.

5.5.2 Drawing a Petri net

It is possible to draw a Petri net without using the GUI.

To perform these actions as part of a script for a PetriNet object pn:

```
import spectral_a
                                                  2
v = spectral_a. Spectral () 3
v. petri_net = pn. petri_net_data 4v.get_petri_net()
                                                  6
## OPTIONAL 7
v. width = \langle \text{width} \rangle ## \text{Default} = 1000 8
v. height = \langle \text{height} \rangle ## \text{Default} = 1000 9
v. border = \langleborder\rangle ## Default = 20 10
v.d_radius = \langle d_radius > ## Default = 60 11
                                                  12
v.\, calculate ( )## set the positions and draw the Petri net the set of \frac{14}{14}
```
5.5.3 Drawing an undirected graph

To draw a graph which is not a Petri net, the graph's *Adjacencymatrix* must be available.

```
import numpy as np 1 and 1 and
import spectral a 2
                                                                  3
v = spectral_a. Spectral () 4
                                                                  5
## OPTIONAL 6
v. width = \langle \text{width} \rangle ## Default = 1000
v. height = \langle \text{height} \rangle ## \text{Default} = 1000
v. border = \langleborder> ## Default = 20 9
                                                                  10
## In this context places refers to a unique identifier for each 11
   vertex in the graph
v . places = np . array ([a', b', 'c', 'd', 'e')]13
## The adjacency matrix is ordered as the places array: 14
## a b c d e 15
v. adjacency = np. matrix ([0, 0, 1, 1, 0], #a
                         \begin{bmatrix} 0, & 0, & 0, & 1, & 1 \end{bmatrix}, #b 17
                         \begin{bmatrix} 1, & 0, & 0, & 0, & 0 \end{bmatrix}, #c 18
                         \begin{bmatrix} 1, 1, 0, 0, 0 \end{bmatrix}, \#d 19
                         [\begin{array}{cccc} 0, & 1, & 0, & 0, & 0 \end{array}] #e 20
v. render graph () 21
```
5.5.4 Save an image of the visualisation

To save an image of a petri net visualisation, a gtk.DrawingArea object needs to be instantiated which is used to represent the visualisation of the graph. The gtk.GraphicsContext, which is bound to the drawing area, is assigned to the petri net via the PetriNet.draw(ctx) method and the petri net components will be drawn onto the drawing area. The drawing area can then be assigned to an instantiation of ExportDrawingArea. Finally, an export method can be called to save an image of the drawing area. Here is code for an example class to carry out these functions:

```
class Export : 1
  """ 2
  Simple example class of how the visualisation of the graph can be 3
    exported to a defined location .
  """ 4
  def \sim iinit = (self, pn):
    """ 6
    Constructor of the sample Export class that defines the basic 7
      setting s for a qtk. Window.
    """ 8
    ## set petri net 9
    self. pn = pn ## pn is a PetriNet object 10## i n s t a n t i a t e a g t k .Window 11
    window = g t k. Window ( ) 12
    ## i n s t a n t i a t e a g t k . DrawingArea 13
    self. \_ \, \text{drawing} \_ \, \text{area} = \text{gtk} \,. \, \text{Drawing} \, \text{Area} ()
    self. drawing area . size (900, 600) 15
    ## embed the drawing area into a viewport 16
    viewport = gtk. Viewport () 17
    viewport . connect ("expose-event", self . update_drawing_area) 18
    viewport.add (self._drawing_area) 19
    ## embed the viewport into the window 20
    window . add ( viewport ) 21
    window \sh{ow} all ()window, show() 23
                                      24def update_drawing_area (self, widget, event): 25
    """ 26
    Update the drawing area in case of an expose event. 27
    """ 28
    \text{ctx} = \text{self}. drawing_area.window.cairo_create() 29
    self._p n.draw(ctx) 30
    \text{ctx } . \text{ clip } () 31
                                      32
  \mathbf{def} \text{ export} (\text{self}): 33
    """ 34
    Export the visualisation of the graph as a PDF to a defined 35
      location .
    """ 36
    ## choose absolute path 37
```


5.6 Calculating the invariants

The *P*- and *T*-invariants of a net are calculated by a sputnik petrinet.PTInvariants() object associated with a sputnik petrinet.PetriNetData() object. The invariants can then be accessed via the p_invariants and t_invariants instance variables of this object. To calculate and display the invariants of a PetriNetData() object, p, issue the following commands:

```
import sputnik<sub>-petrinet</sub>
                                                                 2
i = sputnik_petrinet . PTInvariants () 3i. set_{p}etri_net(p)i. calculate -p invariants ()
i.calculate_t_invariants()
                                                                  7
print i.p_invariants
print i.t_invariants
```
5.7 Running a simulation

Sputnik can simulate Petri nets using either an exact stochastic simulation algorithm (SSA), the Gillespie, or an approximate SSA, the tau leap. Exact SSAs sample the waiting time to each new reaction explicitly, using exact reaction hazards. Approximate SSAs use approximate hazards, sacrificing some accuracy for a shorter runtime. The Gillespie SSA can handle test arcs, inhibitory arcs and capacities, and is the recommended algorithm for most situations (it must be used if knowing the time of occurrence of each and every event is

desired). The tau leap SSA may be used when the model to be simulated involves large species abundances. Under these conditions, the tau leap offers significant speed advantages over the Gillespie, while still providing a very accurate simulation. The tau leap cannot be used with test arcs, inhibitory arcs or capacities.

sputnik simulation.Gillespie() and sputnik simulation.TauLeap() are subclasses of sputnik simulation.Algorithm(), an abstract base class providing the general instance variables algorithm, num_runs, num_iterations, run_time and time_step, plus the general interface method run simulation(). When a simulation algorithm subclass is instantiated, algorithm is automatically set to the correct algorithm type and num runs is initialized as the default value 1. The simulation may be run for a specified num iterations or until a certain time *t* is reached, with output data being stored at regular timepoints. In the latter case, both run time and time step should be set.

Each simulation run initialises an object from the appropriate sputnik simulation.SimData() subclass, namely sputnik simulation.GillespieData() or sputnik simulation.TauLeapData(). Five types of output data are stored in this class:

- *•* times: a 1D NumPy array of timepoints of length *n*
- markings: a 2D NumPy array $(n \times P)$ of net markings at each timepoint
- events: usually a 2D NumPy array $((n-1) \times P)$ of event firing frequencies between each timepoint. For a Gillespie simulation run by iteration, this is a 1D array where each entry gives the index of the event that fired that iteration.
- event freqs: a list (length *T*) giving the total frequency with which each transition fired
- *•* iterations: the number of iterations simulated

Each SimData() object is appended to a list, which is set as the simulation data instance variable of the Gillespie() or TauLeap() object.

5.7.1 Running the Gillespie SSA

```
## I n i t i a l i s e a s im u l a t i o n o b j e c t 1
import sputnik_simulation
g = sputnik_simulation. Gillespie ()
```

```
g. petri_net = p ## p is a PetriNetData object
                                             5
## OPTIONAL set the number of runs if multiple runs are desired 6
g. num\_runs = \langle num\_runs \rangle8
## EITHER choose a number of iterations
g. num iterations = <num iterations > 10
                                             11
## OR set a run time and time step 12
g. run time = <run time> 13
g. time_step = \langletime_step\rangle15
## Run the simulation 16
g. run simulation () 17
output = g.simulation_data 18
                                             19
## You may print the raw data for a particular run (uses zero 20
  indexing)
print output[\langlerun \rangle]. times 21
print output |\langle \text{run} \rangle|.markings 22
print output[\langlerun \rangle]. events 23
print output |\langle \text{run} \rangle|. event freqs 24
print output[\langlerun \rangle]. iterations 25
```
5.7.2 Running the tau leap SSA

There are three additional parameters for the tau leap algorithm compared to the Gillespie. The default values will be suitable in most circumstances. For a full explanation of the algorithm and its parameters, consult Cao *et al.* (2006)^{[\[10\]](#page-43-9)}.

- 1. epsilon (default = 0.03 ; sensible range = $0-0.1$) is a value between 0 and 1 that adjusts the stringency of the algorithm, ϵ . The smaller the value of ϵ , the smaller the calculated values of τ , since ϵ is the maximum permitted relative change in any reaction hazard each timestep.
- 2. control parameter (default = 10; sensible range = $2-20$) determines the threshold place marking that will cause the Gillespie algorithm to be invoked.

3. num ssa runs (default $= 100$) determines how many iterations of the Gillespie algorithm should be run each time the marking of a place drops below the control parameter value.

```
## Initialise a simulation object 1
import sputnik simulation 2 2
t = \text{sputnik-simulation}. \text{Taulteap}()t. petri net = p ## p is a PetriNetData object \frac{4}{4} 4
                                         5
## OPTIONAL set the number of runs if multiple runs are desired 6
t . num runs = <num runs> 7
                                         8
## EITHER choose a number of iterations
t. num iterations = <num iterations > 10
                                         11
## OR set a run time and time step 12
t . run time = <run time> 13
t. time\_step = \langle time\_step \rangle15
## OPTIONAL change the simulation parameters from default the
t. epsilon = <epsilon > 17
t. control parameter = <control parameter > 18
t . num ssa runs = <num ssa runs> 19
                                         20
## Run the simulation 21
t. run simulation () 22
output = t \cdot simulation\_data 23
                                         24
## You may print the raw data for a particular run (uses zero 25
  indexing)
print output[<run >]. times 26
print output[<run >].markings 27
print output[\langlerun \rangle]. events 28
print output[\langlerun \rangle]. event_freqs 29
print output[\langlerun \rangle]. iterations 30
```
5.8 Plotting simulation diagrams

The three classes Trajectory, Diagram and DiagramVisualisation are needed to create a flexible representation of simulation results. A Trajectory object is used to define a single trajectory (place timecourse) and its properties; a Diagram object combines multiple Trajectory objects and defines properties of a diagram or subplot and finally DiagramVisualisation is used to define the actual representation of the defined Diagram objects. The following script is for visualising an Algorithm subclass object sim of a PetriNetData object p.

```
import matplotlib_visualisation
                                                 2
# create a PetriNetData ob jec t p and simulate i t to get sim 3
... 4
                                                 5
# instantiate a general object that includes the single diagrams 6
vis = matplotlib_visualisation. DiagramVisualisation () 7
# set properties
vis . title = <title > 9
vis. legend\_visibility = True 10
vis. \text{ title\_visibleility} = \text{True} 11
\text{vis} \cdot \text{subplots} = \text{True} 12
vis line_width = \langleline width\rangle ## De fault = 1 13
                                                 14
# iterate through all simulation runs 15
for i in range(\langlenum_sims\rangle): 16
  # instantiate an object that combines single trajectories 17
   d_0 obj = matplotlib visualisation . Diagram () 18
  # set properties 19
   d obj. title = "Simulation x'' + str(i + 1) 20
   d_0, d_1 d_2 d_3 d_4 d_5 d_7 d_8 d_1 d_2 d_3 d_4 d_5 d_7 d_8 d_1 d_2 d_3 d_4 d_7 d_8 d_9 d_1 d_2 d_3 d_4 d_5 d_7 d_8 d_9 d_9 d_9 d_9 d_9 d_9 d_9 d_9d_0bj . ylabel = "Markings" 22
   d<sub>-obj</sub>. legend position = 0 23d_{\text{obj}}. title visibility = True 24
   d<sub>-obj</sub>. legend visibility = True 25
  # iteration through all trajectories 26
   for j in range (\text{len}(p.\text{places})):
     # instantiate a trajectory object 28
```

```
t = m \atop t = 0 to t = m \atop t = 0 to t = w is ualisation. Trajectory ()
      # set properties 30
      t_-obj.legend_text = p.places [j] + "---" + d_obj.title 31
      t_0 to t_0 auto color allocation = True 32t_0, x_0 x_0 x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_9 x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_9 x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_9 x_1 x_2 x_3 x_4 x_5 x_6 x_7t = obj. y = data = sim. simulation = data[i]. marks[:, j]) 34
      # add tra jec tory ob jec t to the diagram ob jec t 35
      d obj . add (t obj , t obj . legend text) 36
   # add diagram object to the visualisation object 37
   vis.add(d_obj, d_obj.title) 38
# v isual ise diagrams 39
vis. plot() 40
```
6. Examples

In the following sections, three example systems are analysed using the Sputnik framework. Example 1 is run via the graphical user interface while Example 2 is demonstrated through a command-line terminal. Example 3 is a demonstration of adjusting the graph layout parameters.

6.1 Example 1 : Repressilator

The repressilator is a synthetic biochemical network designed for *Escherichia coli*. The system acts as a cellular clock, exhibiting regular oscillatory behaviour involving three protein-coding genes^{[\[13\]](#page-44-2)}. Figure [6.1](#page-30-2) shows a Petri net representing this network.

Figure 6.1: The Repressilator genetic system.

The program is supplied with the following example file which represents the above Petri net:

```
## Repressilator text file ##
places= [gA, pA, gA_off, gB, pB, gB_off, gC, pC, gC_off]
t = [gA_expression, pA_degradation, pA_inhib_gB, gB_reactivate,
 gB_expression, pB_degradation, pB_inhib_gC, gC_reactivate,
 gC_expression, pC_degradation, pC_inhib_gA, gA_reactivate]
pre arcs= [[1, 0, 0, 0, 0, 0, 0, 0, 0],
 [0, 1, 0, 0, 0, 0, 0, 0, 0],
 [0, 1, 0, 1, 0, 0, 0, 0, 0],
 [0, 0, 0, 0, 0, 1, 0, 0, 0],
                       \begin{bmatrix} 0, & 1, & 0, & 1, & 0, & 0, & 0, & 0, & 0 \ 0, & 0, & 0, & 0, & 0, & 1, & 0, & 0, & 0 \ 0, & 0, & 0, & 1, & 0, & 0, & 0, & 0 \ 0, & 0, & 0, & 0, & 1, & 0, & 0, & 0 \ 0, & 0, & 0, & 0, & 1, & 0, & 1, & 0, & 0 \ \end{bmatrix}, \ \begin{bmatrix} 0, & 0, & 0, & 0, & 0, & 0, & 0 \ 0, & 0,0, 0, 0, 0, 1, 0, 0, 0, 0]<br>0, 0, 0, 0, 1, 0, 1, 0, 0]
                        [0, 0, 0, 0, 1, 0, 1, 0, 0],
[0, 0, 0, 0, 0, 0, 0, 0, 0, 1],[0, 0, 0, 0, 0, 0, 0, 1, 0, 0],[0, 0, 0, 0, 0, 0, 0, 0, 1, 0],[1, 0, 0, 0, 0, 0, 0, 0, 1, 0],[0, 0, 1, 0, 0, 0, 0, 0, 0]post_arcs =[[1, 1, 0, 0, 0, 0, 0, 0, 0],<br>
[0, 0, 0, 0, 0, 0, 0, 0, 0, 0],<br>
[0, 0, 0, 0, 0, 1, 0, 0, 0],<br>
[0, 0, 0, 0, 0, 1, 0, 0, 0],
[0, 0, 0, 0, 0, 0, 0, 0, 0, 0][0, 0, 0, 0, 0, 1, 0, 0, 0] [0, 0, 0, 1, 0, 0, 0, 0, 0],
 [0, 0, 0, 1, 1, 0, 0, 0, 0],
                       \begin{bmatrix} 0, & 0, & 0, & 0, & 0, & 1, & 0, & 0, & 0, \ 0, & 0, & 0, & 0, & 0, & 0, & 0, & 0 \ 0, & 0, & 0, & 1, & 0, & 0, & 0, & 0, & 0 \ 0, & 0, & 0, & 1, & 1, & 0, & 0, & 0, & 0, & 0 \ \end{bmatrix} \begin{bmatrix} 0, & 0, & 0, & 1, & 1, & 0, & 0, & 0, & 0, & 0 \ 0, & 0, & 0, & 0, & 0, & 00, 0, 0, 0, 0, 0, 0, 0, 1]<br>0, 0, 0, 0, 0, 0, 1, 0, 0]
[0, 0, 0, 0, 0, 0, 0, 1, 0, 0], [0, 0, 0, 0, 0, 0, 1, 1, 0],
 [0, 0, 0, 0, 0, 0, 0, 0, 0],
[0, 0, 1, 0, 0, 0, 0, 0, 0][0, 0, 1, 0, 0, 0, 0, 0, 0]<br>
[1, 0, 0, 0, 0, 0, 0, 0, 0, 0]rates = [0.1, 0.001, 1, 0.0001, 0.1, 0.001, 
 1, 0.0001, 0.1, 0.001, 1, 0.0001]
marking = [1, 0, 0, 1, 0, 0, 1, 0, 0]
```
Figure 6.2: A plain text file which specifies the repressilator Petri net model.

To load this input file from the GUI, select open file \Box , then locate and open repressilator.txt, included in the Sputnik package in the examples/ directory.

The Petri net will now be displayed. To calculate *P*- and *T*-invariants, select the invariants icon $\vert \cdot \vert$. The following results window will then appear:

Figure 6.3: Calculated *T*- and *P*-invariants.

The Petri net can now be simulated using the Gillespie alogrithm. To do this, click the simulation icon $\vert\mathbb{X}\vert$, you will then be presented with the simulation configuration options:

Figure 6.4: Configuration options for simulating the firing of a Petri net.

In this example, the runtime has been set to 300,000 and the Step-Size to 500. The Petri net can now be simulated by clicking Start Simulation. An info box will inform the user when the simulation is complete. Before plotting the results, a number of parameters can be adjusted: For the example shown below (Figure [6.6\)](#page-34-1), the Title was changed and Show Legend was deselected, additionally some of the line colors were set manually, using the Specific Plot-Options; to save these changes, click Save Specific Plot Setting, then to visualise the plot, click Show Plot.

Repressilator simulation 140 120 100 80 60 40 20 0^{1}_{0} 50000 100000 150000 200000 250000 300000

Figure 6.5: Graph output of stochastic simulation results for the repressilator Petri net model. The *y*-axis denotes place markings and the *x*-axis shows the runtime. The *red*, *green* and *blue* lines represent the three proteins in the repressilator model.

This graph can then be exported to numerous image formats, including pdf, svg and png.

6.2 Example 2 : Four-reaction system

A second example system, the four-reaction system[\[17\]](#page-44-6), will now be entered and simulated using a command-line interface. These commands can be run using iPython or as part of a Python script.

Figure 6.6: A Petri net representing the four-reaction system.

The first step required is to import specific modules of the Sputnik framework. In this example we will be using the tau-leap simulation method, due to the large number of molecules involved in this system. The required imports are:

The Petri net can now be specified using the following statements (Note the large initial marking used in this example):

```
p = sputnik petrinet . PetriNetData () 1
p. \text{places} = np. \text{array} (['S1', 'S2', 'S3')]p t r ansitions = np . a r r ay (\lceil \n\cdot R_1 \cdot \n\rceil, \lceil \cdot R_2 \cdot \n\rceil, \lceil \cdot R_3 \rceil, \lceil \cdot R_4 \rceil) 3
p. rates = np.array ([1, 0.002, 0.5, 0.04], dtype=float) 4
p. initial\_marking = np.array([100000, 0, 0], dtype=int)
```
Pre and post arcs are stored in a seperate stoichiometry class:

In preparation for Tau leap simulation, the following extra procedures need to be called:

```
s . calculate consumed () 1
s. calculate_species_hors () 2
```
In order to run the simulation three parameters are required, petri net, run time and time step, which can each be set as follows:

 $t =$ sputnik_simulation. TauLeap() $t.$ petri net = p 2 t. run time $= 40$ 3 $t. time_step = 0.01$

Now you are ready to run the simulation and visualise the output:

Figure 6.7: The results of Tau-leap simulation of the four-reaction system. The *x*-axis represents runtime and the *y*-axis shows place markings. Coloured lines are represent places as follows: *blue*: S1, *green*: S2, *red*: S3.

NOTE: for a more sophisticated way to plot diagrams, see section [5.8.](#page-28-0)

6.3 Example 3 : MAP kinase

The library contains two powerful layout algorithms to help the user make sense of Petri nets imported into the program. There are parameters within these algorithms that can be optimised for a given scenario, be it the requirements of a specific graph, or particular drawing area size. To demonstrate how these parameters affect the graph layout process, the MAP kinase model^{[\[18\]](#page-44-7)} will be used, due to its high layout difficulty as a result of its non planar characteristic and high connectivity.

When a new Petri net is loaded to the program it is automatically laid out using the spectral algorithm with default settings. An example of the MAP kinase system under default layout conditions is shown in Figure [6.8.](#page-36-1)

Figure 6.8: The default layout of the MAP kinase system shown here is not ideal, there is some clustering of objects and this has caused some of the object labels to overlap.

By decreasing the border size to provide more space for the layout of objects and increasing the size of the displacement radius to detect more clusters, you can generate a nicer automatic layout. The result of refining the layout parameters for the MAP kinase Petri net is shown in figure [6.9.](#page-37-0)

Figure 6.9: The refined layout of the MAP kinase system shown here has solved some of the problems that are present in Figure [6.8](#page-36-1) such as clustering of objects and the overlap of labels.

To further improve the layout, you can drag objects to the desired location, save the coordinates and lock the Petri net in place shown in Figure [6.10.](#page-37-1)

Figure 6.10: Manually-refined layout. The object highlighted in blue is the object currently being moved by the user.

7. Extending the library

Sputnik was planned and designed using the object oriented paradigm (Figure [7.1\)](#page-39-0). The *PetriNet* class is the heart of the framework, used to encapsulate all the other components from each other. This means that these individual components may be extended seperately, without worrying about how the rest of the program will be affected, so long as the interaction with the central $PetriNet$ class remains the same. In the rest of this section, advice is offered on how to extend aspects of the library.

7.1 Extending the GUI

Sputnik uses the Model-View-Controller (MVC) architecture, which allows the integration of new components into the GUI without major changes to the whole system^{[\[19\]](#page-44-8)}. It consists of three main components: model, view and controller^{[\[19,](#page-44-8)[20\]](#page-44-9)}. *Views* form visual aspects of the GUI and *controllers* manage user interactions with views. Each view and controller is registered with a *model*. In Sputnik, there is only one model, and it manages all the interactions between the views and controllers. The views and controllers are *observers* of the model. If there is a data change in a view or controller object, that object notifies the model of the change, and the model in turn notifies its observers of the same changes, synchronising the current state of the program. Figure [7.2](#page-39-1) shows an overview of the MVC architecture.

Figure 7.1: Simplified class diagram illustrating the overall architecture of Sputnik. Key: group of classes, *module name*, other class names.

Figure 7.2: A general overview of the MVC architecture^{[\[19\]](#page-44-8)}. Views inherit from a general View class, which itself inherits from the MVCObserver class. A *controller* handles user interactions with the view. Both views and controllers are registered at their model, which inherits from MVCObservable. The model carries out the notification protocol, which informs its registered observers of data changes.

The main reasons for choosing the MVC architecture were its extensibility, flexibility and re-usabilty[\[20\]](#page-44-9). Another important factor was its integrated notification protocol, which is used to synchronise the views and controllers during runtime. Extensions to the GUI should abide by MVC practices. The following code presents a sample extension with a new view and controller:

```
import gtk 1
import pygtk 2
                                                       3
import sputnik gui 4
                                                       5
class ViewExtension ( sputnik gui . View ) : 6
                                                       7
   \mathbf{def} \botinit\bot (self): 8
      ## c a l l c o n s t r u c t o r o f p a ren t c l a s s 9
      sputnik gui . View . __ init __ (self) 10
                                                       11
   def \sim .init = (self, model = None, controller = None):## call constructor of parent class 13
      sputnik_gui.View.__init__(self, model, controller) 14
                                                       15
   ## common methods which are used for displaying and notification is
      purposes
   def show(self):\mathbf{p} assess the contract of the contract 
   def update_component (self, key): 19
      \mathbf{p}ass 20def update output ( sel f ) : 21
      pass 22
   \det \text{undo}(self): 23
      pass 24
   def update (self): 25
      \mathbf{p}ass 26def reset (self): 27
      pass 28 and 28
                                                       29930
class ControllerExtension ( sputnik gui . Controller ): 31
                                                       32
   def \sim iinit = (self): 33
      ## call constructor of parent class 34
      sputnik_gui. Controller. __init__(self) 35
                                                       36
   def \sim \text{unit} - (self, model = None, view = None): 37
      ## call constructor of parent class 38
      sputnik_gui. Controller . \text{__init}_ (self, model, view) 39
                                                       40
   ## common methods which are used for displaying and notification and
      purposes
   def show(self): 42
      pass 43
   def update_component (self, key): 44
      pass and the contract of the
   def update_output (self): 46\mathbf{p}ass and the contract of the contract 
   \mathbf{def} \text{ undo} (\text{self}):
      pass 49 and 49
   def \ update(self):\mathbf{p}ass \mathbf{p}\mathbf{def} \ \ \mathbf{reset} \ (\ \mathbf{self} \ ) : \{\bf pass} 53 {\bf 53}
```
7.2 Adding additional language support

It is simple to extend the range of file formats accepted by Sputnik. To do this, a single lexing class should be added (which could optionally be based on any of the existing classes RLexerTxt, RLexerSBML or RLexerPNML). The only requirement of a novel lexing class is that it returns a list of token objects, defined in the Token class, so that they can be correctly parsed through RParser. Accepted components of a token list are detailed below (Table [7.1\)](#page-41-1). It is also possible to instantiate a *PetriNetData* object directly, bypassing tokenisation and parsing; this method will, however, also avoid existing error-handling and input constraints so should be used with caution.

Token.label	Token.value
$, p, \$	np.array of place names
$, +$	np. array of transition names
,r	np. array of rate constants
, m	np. array of initial markings
, c,	np. array of capacities
'pre'	np.matrix for pre
'post'	np.matrix for post
'test'	np.matrix for test arcs
'inhib'	np.matrix for inhibitory arcs

Table 7.1: All possible components of a Token list. np refers to the numpy module.

Existing error checking methods can be invoked on any newly-defined lexer class by inheriting from class RLexer and calling the function self.check(), passing the completed token list as an argument. Alternatively, in-built error checking can be avoided by omitting this function call.

A new lexing class could be incorporated into the GUI frontend by editing the controller main.py file. First, the new module should be imported in the file header. Then the open file function should be edited to initialise the new lexer upon the opening of a file with the required extension. For example:

```
if '. yourfileextension' in f.name:
   lexer = newModule.newLexerClass()
```
In order to save to a novel format, a converter class can be written which extracts data from a PetriNetData object and writes to a file format of choice. This functionality can then be added to the GUI as above, but instead editing the open file function.

7.3 Adding additional simulation algorithms

To add an additional simuluation algorithm, simpy create a new subclass of the abstract base class Algorithm. This new class should contain a method that runs the simulation, and a class variable, algorithm, whose value is the same as the name of the simulation method. The simulation method should return data in a format consistent with that of the existing algorithms, and store it in a new subclass of the abstract base class SimData.

References

- [1] CA Petri. Kommunikation mit automaten. *Bonn: Institut fur Instrumentelle Mathematik, Schriften des IIM*, 3, 1962.
- [2] R. David and H. Alla. *Discrete, Continuous, and Hybrid Petri Nets*. Springer-Verlag Berlin, 2005.
- [3] M. A. Marsan. Stochastic petri nets: An elementary introduction. In *In Advances in Petri Nets*, pages 1–29. Springer, 1989.
- [4] D. Wilkinson. *Stochastic Modelling for Systems Biology*. Chapman & Hall / CRC Mathematical & Computational Biology, 2006.
- [5] J. W. Pinney, D. R. Westhead, and G. A. McConkey. Petri net representations in systems biology. *Biochemical Society Transactions*, 31:1513–1515, 2003.
- [6] D. Gilbert, M. Heiner, and S. Lehrack. A unifying framework for modelling and analysing biochemical pathways using petri nets. Technical report, Brandenburg University of Technology at Cottbus, 2007.
- [7] P.J.E. Goss and J. Peccoud. Quantitative modeling of stochastic systems in molecular biology by using stochastic petri nets. *Proceedings of the National Academy of Sciences of the United States of America*, 1998.
- [8] T. Toni. *Approximate Bayesian computation for parameter inference and model selection in systems biology*. PhD thesis, Imperial College London, 2010.
- [9] D. T. Gillespie. Exact stochastic simulation of coupled checmical reactions. *Journal of Physical Chemistry*, 81(25):2340–2361, December 1977.
- [10] Y. Cao, D. T. Gillespie, and L. R. Petzold. Efficient step size selection for the tau-leaping simulation method. *J Chem Phys*, 124(4):044109, Jan 2006.
- [11] A. Finney and M. Hucka. Systems biology markup language: Level 2 and beyond. *Biochem Soc Trans*, 31(Pt 6):1472–1473, Dec 2003.
- [12] Pnml.org. Pnml grammar, version 2009, 2009.
- [13] M. B. Elowitz and S. Leibler. A synthetic oscillatory network of transcriptional regulators. *Nature*, 403:335–338, 2000.
- [14] Creative Commons Attribution-ShareAlike 3.0 Unported Licence. http://creativecommons.org/licenses/by-sa/3.0/.
- [15] Open Source Icons. http://openiconlibrary.sourceforge.net/.
- [16] PyDoc Python v2.7.2 Documentation. http://docs.python.org/library/pydoc.html.
- [17] T. Tian and B. Burrage. Binomial leap methods for simulating stochastic chemical kinetics. *Journal of Chemical Physics*, 121:10356–10364, 2004.
- [18] T Toni, Y Ozaki, P Kirk, S Kuroda, and MPH Stumpf. Elucidating phosphorylation dynamics of the erk map kinase (in preparation).
- [19] F. Buschmann, R. Meunier, H. Rohnert, P. Sommerlad, and M. Stal. *Pattern - Orientierte Software Architektur: Ein Pattern - System*. Addison-Wesley, 1998.
- [20] E. Gamma E and J. Vlissides R. Helm, R. Johnson. *Design Patterns: Elements of Reusable Object-Oriented Software*. Addison - Wesley, 1 edition, 1994.